THE ROLE OF THE TRANSITION STATE BOND ORDER AND REACTION **ENERGY IN METHYL NUCLEOPHILIC SUBSTITUTIONS**

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Abstract - A general intersecting-state model has been applied to the calculation of the energy barriers for methyl nucleophilic substitutions in vapour phase and solution in terms of force constants and lengths of reactive bonds, reaction energy and the bond order of the transition state, n^{\ddagger} . In the vapour phase the current reactions have been found to have a n^{\pm} value close to unity $(n^{\pm}=0.93)$. This is attributed to the involvement of a pair of nonbonding electrons of the substituents, which acquires a movement of a the transition state. In liquid solutions such a pair of electrons is not completely available to increase $n^{\frac{1}{2}}$, due to interactions with solvent molecules. The calculated values depend on the hard-soft nature of the substituents and the accepting properties of the solvent being higher for soft groups and solvents of low acceptor number. Solvent effects on reaction rates are interpretable in terms of the effect of solvent polarity on the transition state bond order and the reaction energy. Vapour phase reactions with delocalized nucleophiles have been found to have n^{\pm} =3/2 and the reaction energy has an inverted effect on the energy barriers, in contrast with the current reactions where this effect is a normal one.

The classical S_N2 nucleophile substitution on methyl substrates is still a very active field of research in physical organic chemistry in spite of a considerable number of experimental and theoretical studies^{1–6} since the basic work of Hughes, Ingold and Patel in 1933.⁷ A renewed interest recently arose for the development of approaches to interconnect the well known solution data with the more recent findings in the vapour phase.¹ With this aim several theoretical calculations have been carried out through ab initio approaches or even with simple models such as the theory of Marcus. To unravel trends of reactivity within a family of related molecules, theoretical models, which sacrifice rigour to gain simplicity, are often better than theab initio calculations. Simple theoretical models such as that of Marcus are therefore particularly adequate in physical organic chemistry. Furthermore it was shown by Wolfe et al.⁸ that the calculations of the Marcus barriers from the intrinsic self-exchange barriers and the exothermicity of the reactions, are in excellent agreement with the ab initio calculations. However, it remains to be understood the large variation (ca. 120 kJ mol⁻¹) in the intrinsic energy barriers, and why such reactions should show as dramatic solvent effects.⁶ With this aim we have applied a recently developed intersecting-state model⁹ to unravel some mechanistic aspects of nucleophilic displacements on methyl. This model which encompasses Marcus and BEBO theories as particular cases, and gives a simple rationale for the Hammond postulate and the linear free energy relationships, has provided some new insights on the mechanisms of these reactions.

Theoretical Model

The theory has been described in detail elsewhere⁹ and only the essential will be stated here. Aliphatic nucleophilic substitutions involve the making and breaking of one chemical bond. Let us assume that the potential energy curves of these reactive bonds can be represented by harmonic oscillators. Within an intersecting-state model the transition state corresponds to the crossing point of the harmonic curves and one can write

$$
(1/2)f_{\mathbf{r}}x^2 = (1/2)f_{\mathbf{D}}(d-x)^2 + \Delta E^{\mathbf{O}} \tag{1}
$$

where fi are the stretching force constants, AEO Is the **reaction energy, x Is the bond extension of the reactant** and d is the displacement of the minima of the potential energy curves. The parameter d represents also the sum of the bond extensions of reactant and product, $d = (l^{\frac{1}{2}} - l_1) + (l^{\frac{1}{2}} - l_0)$. The activation energy of the reaction **is given by**

$$
\Delta E^{\frac{1}{2}} = (1/2) f_r x^2 \tag{2}
$$

where x is estimated from eq (1) once d is known. The sum of the bond extensions was shown9 to be proportional to the sum of the equilibrium bond lengths of reactant and product

$$
d = n(l_r + l_p) \tag{3}
$$

where n is the reduced bond extenslon. This equation has a slmple physlcal meaning: when an equilibrium bond length is small its bond extension is small, but when it is large, the bond extension is also large.

The parameter n is related to the chemical bond order at the transition state, n[‡], and to the so called **%onfiguration entropy", A, proposed by Agmon and Levine.10**

$$
\eta = \frac{a' \ln 2}{n^{\frac{1}{2}}} + \frac{a'}{2} \left(\frac{\Delta E^O}{\lambda}\right)^2 \tag{4}
$$

 a' is a constant ($a' = 0.156$) and λ has the dimensions of an energy.

In eq (4) the first term a'ln2/n[‡] allows one to estimate the intrinsic energy barriers at $\Delta E^{\circ} = 0$. The second **term takes Into account any effect of the reaction energy on the displacement d of the potential energy curves. At the transition state, tha reaction energy has to be accommodated Internally. If the activated complexes have** few ways and, consequently, a small capacity to store ΔE^O ($\lambda < |\Delta E^O|$) this energy has to be stored in the **reactive bonds, through further bond extensions. In consequence n and d both Increase with an increasa In** lAE"I. However if the activated complexes have many ways and a large capacity to store energy (x>>|AE°|) then **no reaction energy will be stored In the reactive bonds and d Is Independent of** AEo. **The latter situation corresponds to the theory of Marcus.**

For vapour phase reactions Involving the making and breaking of the chemical bonds of dlatomlc molecules, the present model gives a good estlmatlon of the activation energy of chemical reactions for one stretching mode in reactants and one in products. However for reactions of complex molecules In the gas phase or for reactions in condensed media, there are many more degrees of freedom. These can be treated on a statistical basis using free energies, and in eqs (1). (2) and (4) E should be substituted by C.

When there is conservation of the total bond order along the reaction coordinate, the transition state bond order is $n^* = 1/2$ (at $\Delta G^0 = 0$) because for single bonds $n_1 + n_r = 1$. However when the reactant or the product possess nonbanding or antlbonding electrons **in low energy molecular orbltals, such electrons can acquire a bonding character at the transition state and n* increases. For example, for hydrogen transfer reactions In** the vapour phase, such as $H + HX + H_2 + X$, where X is an halogen atom which possess pairs of nonbonding **electrons, one of such pairs can acquire a bondlng character at the transitlon state and then n* =l.g This nonconservation of the bond order of the chemical reactlonr can be viewed in terms of simple molecular orbital** diagrams¹¹; for $\{HHX\}^{\pm}$ the electronic configuration $1\sigma^2$ $2\sigma_{\rm K}^2$ $2\sigma_{\rm K}^2$ (σ) and σ and τ = 1 for each one of the chemical bonds. For a reaction $H + X_2 + HX + X$ the halogen diatomic molecule possess a pair of **antlbondlng electrons which acquires a bonding character at the transition state and the average bond order of** the two transition state bonds is $n^{\ddagger} = 3/2.9$

In our model both parameters $n^{\frac{1}{2}}$ and λ allow one to define the concept of a reaction series. A series of similar reactions is characterized in terms of a constant n^{\ddagger} and λ .

Gas phase reactions

Brauman and coworkers^{3,4} have undertaken a kinetic study of the react<mark>ions of s</mark>everal anions with methane derivatives in the vapour phase. The rates of reaction, k_r, are smaller than the rates of collision. We have considered the reactions as concerted processes with an activation free energy barrier given by $k_r = k_c$ **exp(-bC*/RT). With such values, d and n values which reproduce AC* can be estimated from eqs (1) to (3) (Table 1); the force constant and bond length data were taken from ref. 12. Since the reactloos tmder study are very** exothermic processes, reasonable fits can be obtained for the normal and the inverted region (AGO<-f_pd²/2). To distinguish between these two possibilities we have to examine the quadratic dependence of n on \triangle C^O, **predlcted by eq (4).**

Figure 1 presents the linear relationship between η and $(\triangle G^o)^2$ in the normal region for several current nucleophilic substitution reactions of CH₃Y. The intercept is n(o)=0.116, which corresponds to a transition state bond order close to unity $(n^{\frac{1}{2}} = 0.93)$. In the inverted region the intercept is much lower, $n(\alpha) = 0.055$ and n^{\pm} = 2. The presence of X or Y groups with nonbonding electrons lead one to expect a transition state bond **order of unity9 and consequently we consider that the reactions 1 to 7 of Table 1 have a normal free energy** dependence $(AG^{\circ} > -f_p d^2/2)$.

aData of ref. 3 except where stated otherwise; ΔG^{\ddagger} estimated from the reaction efficiency; **R** Assumed to be identical to ∆H^o; L 1=(l_r + I_p) ; L Reactions with inverted region behaviour (a to h); L Data of **ref. 4; &J mol-T A*2; g kJ mol-1.**

Other reactions (a to g on Table 1) do not follow the same dependence of Figure 1, and consequently represent a different reaction series. Such reactlcns are also associative processes, but involve delocalized nucleophiles.³ These reactions do not follow the linear dependence of η on (ΔC^{O)2} in the normal region. **However, such a dependence is found in the inverted region (Figure 2). The Intercept n(o) = 0.071 corresponds** to the type-III $(n^{\frac{1}{2}} = 3/2)$ hydride reactions since $n^{\frac{1}{2}} = 1.52$. Another pair of electrons from the delocalized **nucleophiles Is siphoned Into the reactive bonds of the activated complexes. With stitituted aromatic nucleophiles further electron slphoning can occur at the transition state as we have shown with sigmatropic shift reacticms.13 This is particularly notable with m-CN-ArCHj.**

All these facts support the view that the energy barriers for the methyl transfer reactlons with delocalized nucleophiles are due to an inverted region effect. Under normal conditions we would have expected that these reactions would be faster than those previously considered, but a decrease in d due to an increase in n^{\ddagger} . moves the reaction from the normal to the inverted region and increases the energy barrier. This is the first **case that we are aware of an inverted region effect, for reactions outside the field of electron transfer processes.**

The values of λ for the reactions of Figures 1 and 2 are quite high $(\lambda = 580 \text{ kJ mol}^{-1}$ and 960 kJ mol⁻¹) when compared with the ones for the hydride reactions (145 to 77 kJ mol⁻¹).⁹ This implies that the dependence of **n on AGO Is very weak for methyl transfers and that the activated complexes are not very tight.**

extensions, n_i , and (ΔG^0) for methyl **transfer reactions in the vapour phase. Legend for the reactions in Table 1.**

Figure 1. Linear dependence of the reduced Figure 2. n versus $(\Delta G^O)^2$ for methyl transfers extensions, η , and (ΔG^O) for methyl **with delocallzed nucleophiles; bottom plot: inverted region; top plot: normal region. Legend in Table 1.**

Brauman et al.3.4 have interpreted the gas phase methyl transfer reactions in terms of the theory of Marcus on a double minimum potential energy surface. For very exothermic reactions this situation can be represented by the following kinetic scheme

$$
X^+ + CH_3Y \underset{k_{-c}}{\overset{k_c}{\rightleftarrows}} X.CH_3.Y^{-} \overset{k_1}{\leftarrows} XCH_3 + Y^-
$$

where X.CH3.T represents a large-dipole complex which can be observed under certain condltions.14 The observed rate constant is simply $k_{obs} = k_c k_1/(k_c+k_1)$. When $k_1 \ll k_c$ it is $k_{obs} = k_c k_1/k_c$ and k_{obs} $=$ A expl- $(AG_{n+1}^+AG_{n+1})/RT$ where A is a preexponential factor, AC_{n+1} is the energy of the intermediate complex and ΔG_{int}^2 the activation free energy for the decomposition of the same intermemediate. As long as **the presence of** the **Intermediate does not alter the energy of the transition state, the apparent activation free** energy with respect to reactants is simply $\Delta G^{\dagger} = \Delta G^{\dagger}_{int} + \Delta G_{int}$ and the formation of the intermediate complex **will not be revealed In the apparent energy barriers of the reaction*. However the formation of such an intermediate can have some effect on the synchronous nature of the reaction.**

Conservation of total bond order, n_r + n_p = 1, is only valid for synchronous processes.¹³ The loss of the synchronous character of the reaction would lead to n_r + n_p < 1 and consequently the transition state bond order will have n^* < 1/2. When there is an increase in the total bond order at the transition state, $n_r + n_p = m$ (m>1), the loss of the synchronous character of the reaction would lead to n_r + n_p <m. For the normal methyl **transfer reactions the transition state bond order is not urity, but slightly smaller (n* = 0.93). Although thls** may be due to the relatively small experimental errors in ΔG^{\ddagger} , it seems more likely that it corresponds to some **loss of the synchronous character of the normal methyl transfer reactions and consequently, to the formation** of a weakly stable intermediate complex with k₁, comparable to k_c. Under this assumption, e.g. for the complex $(CH_3O, CH_3Br)^{-}$ the binding energy is estimated to be $AG = -1.7$ kJ mol⁻¹ (300 K) in agreement with the accepted view that, along the reaction path, there is a double-well potential with an energy barrier. The value of the potential-well is comparable to values calculated by Carrion and Dewar⁶ for similar complexes. **The scatter of polnts in Figure 1 can also be due to small differences on the binding energy of these charge-dipole complexes.**

 5 The same conclusion stands even when k_1 is comparable to k_{-c} , as long as the intermediate charge-dipole **complex cannot dissipate Its excess energy fast enough In the gas phase.**

Reactions in Water

Several methyl transfer reactions have been studied in water solutions. Albery and Kreevoy² have reviewed these data which can be studied in the same manner as the vapour phase processes. Table 2 summarizes the calculated data. With the exception of the very exothermic processes (CN⁻ and OH⁻), the calculated reduced displacements are essentially free of the quadratic dependence on AGO, and can be used to calculated the bond orders at the transition state through eq (4), $n(o) = 0.108/n^{\frac{1}{2}}$. The results are also presented in Table 2.

<u> a Data from ref 2; b Extrapolated to ∆G^o = 0; <u>£</u> kJ mol⁻¹ A^{o-2}; **d** kJ mol⁻¹</u>

the change in n^{\ddagger} . The most striking feature that comes from comparison with vapour phase data is Whereas for the normal reactions in the vapour phase $n^{\frac{1}{2}} \approx 1.0$, in water solutions $n^{\frac{1}{2}}$ is close to 0.5. As we have said before, $n^{\frac{1}{2}} \approx 1.0$ is attributed to a siphoning of the electronic density of the pair of nonbonding electrons of a halogen or oxygen atom into the transition state. The fact that in water $n^{\frac{1}{2}} = 0.5$ reveals that such nonbonding pair of electrons, owing to strong interactions with the solvent, is not available to increase the total bond order of the transition state. Although this is the main feature for these reactions, there are significant differences between the substituents.

Table 3 summarizes the n⁺ values for several substituents. The conclusion that we can establish is that the availability of the nonbonding pair of electrons, which becomes a bonding pair at the transition state, is in the order $F^-(H_2O) < CI^- < Br^- < I^-$. Consequently, soft anions favour the nucleophilic substitutions from an electronic point of view, whereas the hard nucleophiles do not help the reactions in solution, because they do not increase the bond order of the transition state. The smaller anions have the higher HOMO which are then more available for the interaction with the H₂O molecules.¹⁵

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The terms "hard" and "soft" have been criticized because of their imprecision and the difficulty of defining them quantitatively.¹⁶ We have attempt to correlate $n^{\frac{1}{2}}$ with some quantitative properties of the entering and leaving groups. A reasonable non-linear correlation has been found for F⁻, C1⁻, Br⁻ and I⁻ with the oxidation **potential. For the same groups there is a linear correlation between n* and one of the empirical Swain-Scott Parameter* nCH3i fnCH3i = log(kCH3I+Y/kCH3l+cH3oH). l7 Both correlations are independent of the group** entering or leaving situation. However when one includes other ions such a NO₃, OH⁻, CN⁻ they do not fit into **any of the previous correlations.**

Steric effects in spin exchange processes of transition metal complexes have been found to cause large vsriatlons in the transition state bond order n*, which lead to variations in rates by several orders of magnitude.'8 In a simliar manner one can interpret the steric effects in alkyi substitutions. For example, fCH313CH2X is about 10-7 times slower than the methyl system. lg Owing to steric hindrances bond-making and bond-breaking processes cannot take place in unison and the synchronous character of the reaction Is lost.

Although data on very exothermic reactions in solution are not so abundant as in the vapour phase, the dependence of n on $(\Delta G^o)^2$ shows that the configuration entropy parameter in solution ranges between λ = 180 **to 250 kJ moi-l. These values are smaller than the ones in the vapour phase which reveals that the activated complexes are more tightly bound species in solution than in gas phase. This involves not only the reagent and product species, but also the solvent molecules of the soivation shell.**

Methyl transfer reactions have been found to obey the Marcus equation.2-5 According to the intersecting-state model, Marcus theory corresponds to the situation where d and n are independent of AGO. This requires high configuration entropies or small $|\Delta G^o|$, a situation that is quite common for the vapour phase **and solution reactions. However a word of caution should be made with respect to the use of cross-reaction rate** constants employed in the Marcus theory. This procedure is only valid when n depends weakly on AG^o and **n* does not vary significantly for the different reactions.**

Solvent Effects

The nature of solvent has a strong influence on the rates of nucleophiiic substitution reactions.20 For example, the S_N2 displacement (charge type 2)

$$
(CH_3CH_2)_3N + CH_3CH_2I + (CH_3CH_2)_4N^+ + I^-
$$

proceeds faster in aichools than in hydrocarbons. In contrast substitution reactions between a negative or positive ion and a neutral molecule (charge type 1 and type 4) and between ions of opposite charges (charge type 3) proceed more rapidly in nonpolar than in polar solvents and, namely, are slowed by addition of water. The present model can provide some insights on these facts.

Table 4 presents the calculated bond extension parameter for methyl nucleophiiic substitutions in non-aqueous solvents and Table 5 shows the corresponding transition state bond orders. According to the present model the higher n[‡] values should be found for solvents with poor accepting properties²¹, such as acetone **(acceptor number, (AN = 12.5) and dimethylformamide (AN = 16). Good acceptor solvents such as water (AN** $=$ 55) and methanol (AN $=$ 41) would lead to low $n^{\frac{1}{2}}$ values, close to the $n^{\frac{1}{2}}$ = 0.5 limiting value.

Solvent	x^-	Υ"	$f_r/10^3$ s	$f_p/10^3$ Ω	$AC + D$ d	AGO D. d	1/A ^o	n
acetonitrile	Br^-	CI^-	2.2	1.9	79	12	3.705	0.145
methanol					109			0,174
DMF ^a					97	22		0.157
methanol	ı-	$C1^-$	2.2	1.6	104	0	3.974	0.169
DMF					92	22		0.148
acetone					89	20		0.146
methanol	r	Br^-	1.9	1.6	90	-6	4.145	0.159
DMF					72	$\mathbf 0$		0.140
acetone					74	10		0.136
methanol	ı-	ı-	1.6	1.6	87	$\mathbf 0$	4.414	0.150
acetone					68	\bullet		0.132

Table 4. Bond Extensions for Methyl Transfer Reactions in Nonaqueous Solvents,

<u>^aDimethylformamide; **b**</u> Data collected in ref 2; **GkJ** mol⁻¹ A^{o-2}; **Indepty**

Table 5. Transition State Bond Orders for Methyl Transfer Reactions in Different Solvents.

The quantitative assessment of the effect of thermodynamics on the reaction rates of methyl transfers has dominated the more recent studies of these systems. The present model has revealed the effect of many other structural factors on the reaction rates, namely the effect of bond lengths and force constants of the reactive bonds, the configvation entropy and the bond order of the trensltlon state. Of all those factors, the important ones are In general, the reaction energy, AGO, and the transition state bond order, n*. In charge type 2 reactions an increase in solvent polarity decreases drastically AG^O, which becomes the dominating effect. **Consequently, the rates increase wlth an increase in solvent polarlty. In contrast, the transitlon state bond order** seems to be the dominant factor for the other charge type reactions. Since n[‡] decreases with increase in **the solvent acceptor number and consequently, with an increase in solvent polarity, the rates are slower for the** more polar solvents.

For some reactions solvents have only a minor effect on the reaction rates, a kind of solvent paradox.6 This is a consequence of the almost equal effect of n[‡] and ΔG^0 on the reaction barriers. A good acceptor solvent **on decreasing both n* and AGO leads to opposlte and compensating effects of both parameters on the reaction barriers.**

In qualitative terms the nucleophilicity of halide ions for reactions in dipolar protic solvents is $\Gamma >$ Br⁻> CI^- > F⁻ reflecting the dominant effect of $n^{\frac{1}{2}}$. In the dipolar aprotic solvents and in the vapour phase ²²the **order is reversed, F- > CI- > Br- > I-, which reveals that other structural factors rather than n[‡] dominate

the reaction kinetics. This is obvious in the vanour phase, because n[‡] is the reaction kinetics. This Is obvlous in the vapour Phase. because n* Is constant for all those substituents.**

In liquid solutions the nucleophillclty can depend on the nature of the halide counter ion. For example the order of reactivity of the halides towards n-butyl brosylate²⁰ in acetone is Cl⁻ > Br⁻ > I⁻ when $(C_AH_Q)_AN^+$ is the cation of the halide salt, but is $I > Br^- > CI^-$ when LI^+ is the cation. A hard cation such as Li^+ interacts more strongly with the hard anions in the ion-pairs and can reverse the order of reactivity, the variation of r[}] **being the dominant factor.**

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